

Academic Scholarship 2012

Preliminary Examination

MATHEMATICS

Time Allowed: 1¹/₂ hours

- Calculators may NOT be used.
- Write your answers on **lined paper** and **show as much working as possible**. <u>Answers without clear logical working will gain little credit</u>.
- Do not spend too long on any single question. If you are having difficulty with a particular question, move on and return to it at the end if you have time. Do not be concerned if you cannot answer all of the questions.
- At the end of the examination, hand in both the question paper and your answers with your name clearly indicated on all sheets.

1. Work out

- (a) 40% of 350. (b) 240 × 25 (c) 5³ (d) $\sqrt{64}$ (e) $3\frac{1}{2} \times 1\frac{1}{3}$ (f) $\frac{\frac{3}{5} - \frac{1}{4}}{\frac{7}{8} \div \frac{1}{4}}$ (g) $\frac{2}{3} \times 12 + 3 \div 0.2$
- 2. (a) Remove brackets :

$$2(3-4x)$$

(b) Factorise fully :

$$6xy^2 - 12x^2y$$

(c) Multiply out the brackets and simplify :

$$(x+3)(x+2)$$

(d) If a = 2, b = -3 and $c = \frac{1}{4}$, work out the value of :

(i)
$$a^2 - b^2$$
 (ii) $\frac{a}{c} - b$ (iii) $-\frac{2}{3}abc$

- 3. Solve for x:
 - (a) 5x 3 = 9 x

(b)
$$\frac{2}{3}(2x-3) = 8$$

4. Solve for *x* and *y* : 2x - 3y = 13

$$3x + 2y = 0$$

- 5. A rectangle has adjacent sides of length (2x + 3) cm and (5x 1) cm. The perimeter is 102 cm. Find the value of x.
- 6. The best sprinters in the world run the 100 metres in about 10 seconds.
 - (a) Work out their average speed during the race in kilometres per hour (km/h).
 - (b) Using a simple conversion (of kilometres to miles), work out their approximate average speed in miles per hour (mph).
- 7. A class of 8 pupils sat an Algebra test. Their average mark was 65%. Jenny was absent for the test, but sat it the following day. When her mark was included, the class average was 60%. What was her mark for the test ?
- 8.



Diagram not accurately drawn.

The diagram shows three squares of the same size. What is the size (in degrees) of the angle marked x?

- 9. James is a property developer. He bought two homes and sold them both a year later. He sold each of them for £ 990 000. On the first home, he made a profit of 10%, but on the second home he made a loss of 10%. Overall, what percentage profit or loss has he made on the two houses, or was his profit/loss exactly zero ?
- 10. When a barrel is 30% empty, it contains 30 litres more than when it is 30% full. How many litres does the barrel hold when it is full ?
- 11. (a) Three <u>different</u> Mathematics books are to be placed side by side on a shelf, as shown below :



Let's call the books A, B and C. Using these letters, write down all the different ways in which the books can be placed.

(b) I now add a fourth Mathematics book (call it D) to the collection. Work out the number of different ways in which the four books can be arranged on the shelf.

(note : you will not get full marks by just writing out all the different ways and counting them – try to think of a clever method of calculating the answer, and remember to show your working so that your method is clear).

(c) Six <u>different</u> Mathematics books are to be placed on a shelf, as shown below.



- (i) In how many different ways can this be done?
- (ii) I now decide that two <u>particular</u> books must occupy the two 'end' positions (marked with a * below). (note : it does not matter which goes on which end).



In how many different ways can I now arrange the books ?

12. At a holiday camp, the ratio of boys to girls is 3 : 4. The ratio of girls to adults is 5 : 7. What is the ratio of children to adults at the camp ?



In the diagram, triangle *XYZ* is isosceles, with XY = XZ. Three angles have been labelled as *r*, *p* and *q*. Find the size of *r* in terms of *p* and *q*.

14. Find the value of
$$\frac{1}{x+2}$$
 if $\frac{1}{x} = 3.5$

15. In Mathematics, n! is called n factorial and this is how it works :

$$n! = 1 \times 2 \times 3 \times 4 \times \dots \times n$$

So, for example :

 $3! = 1 \times 2 \times 3$ and $7! = 1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7$

Amazingly, the exact number of seconds in 6 weeks is equal to b! (*b* is a whole number).

Work out the value of *b*.